

Worksheet 3: Properties of Coarse-grained Polymers

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June 3, 2015

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General Remarks

- Deadline for the report is **Monday, 15th of June 2015, 12:00 noon**
- In this worksheet, you can achieve a maximum of 20 points.
- The report should be written as though it would be read by a fellow student who attends the lecture, but doesn't do the tutorials.
- To hand in your report, send it to your tutor via email.
 - Johannes (zeman@icp.uni-stuttgart.de) (Thursday 14:00-15:30)
- Please attach the report to the email. For the report itself, please use the PDF format (we will *not* accept MS Word doc/docx files!). Include graphs and images into the report.

- The report should be 5–10 pages long. We recommend using L^AT_EX. A good template for a report is available online.
- The worksheets are to be solved in **groups of two or three** people.

1 Introduction

In the first part of this worksheet, you will have to answer a few general questions about coarse-grained polymer models and solve a related mathematical task.

In the remainder of the worksheet, you will get to know our in-house software package ESPResSo (Extensible Simulation Package for Research on Soft matter). Using ESPResSo, you will perform several simulations involving coarse-grained polymers and analyze their properties.

All files required for this tutorial can be downloaded from the lecture's homepage.

2 Short Questions - Short Answers (6 points)

Task	(6 points)
Answer the following questions:	
<ul style="list-style-type: none">• What is the persistence length of a polymer and how is it defined?• Which real polymers can be described by the worm-like chain model?• What are the differences between the ideal chain, the worm-like chain, the freely jointed chain and the self-avoiding chain?	

Hint

- You might want to study literature to answer these questions. A good reference would be the book *Polymer Physics* by Rubenstein.

3 Polymer Properties (6 points)

Consider an ideal linear chain with N Kuhn monomers of length b and fixed end-to-end vector \mathbf{R} directed along the x -axis.

Task

(6 points)

- Demonstrate that the mean square projection of the radius of gyration onto the direction of its end-to-end vector is

$$\frac{1}{N} \sum_{i=1}^N \langle ((\mathbf{r}_i - \mathbf{r}_{\text{com}})_x)^2 \rangle = \frac{1}{36} N b^2 \left(1 + \frac{3\mathbf{R}^2}{Nb^2} \right), \quad (1)$$

where \mathbf{r}_i is the position of the i -th monomer and \mathbf{r}_{com} is the position of the polymer's center of mass.

- Show that the mean square projection of the radius of gyration onto the perpendicular direction is independent of the magnitude $|\mathbf{R}|$ of the end-to-end vector:

$$\frac{1}{N} \sum_{i=1}^N \langle ((\mathbf{r}_i - \mathbf{r}_{\text{com}})_y)^2 \rangle = \frac{1}{N} \sum_{i=1}^N \langle ((\mathbf{r}_i - \mathbf{r}_{\text{com}})_z)^2 \rangle = \frac{1}{36} N b^2 \quad (2)$$

Remarks

Note that

- for $|\mathbf{R}| = 0$, the mean square radius of gyration of a ring polymer $\langle R_g^2 \rangle = \frac{Nb^2}{12}$ is recovered,
- for $|\mathbf{R}| = b\sqrt{N}$, the mean square radius of gyration of an ideal linear chain $\langle R_g^2 \rangle = \frac{Nb^2}{6}$ is recovered,
- and for $|\mathbf{R}| = bN$, the mean square radius of gyration $\langle R_g^2 \rangle = \frac{1}{12} N^2 b^2$ is recovered in the limit of large N .

It is interesting to point out that the asymmetry of the ideal linear chain $\left(1 + \frac{3\mathbf{R}^2}{Nb^2}\right)$ is quite large and a typical shape is better represented by an elongated ellipsoid than by a sphere.

4 Static Properties of Coarse-grained Polymers with ESPResSo (8 points)

4.1 The Software Package ESPResSo

The software package ESPResSo is developed and maintained at the Institute for Computational Physics and is mainly intended to perform coarse-grained simulations with Lattice-Boltzmann (LB), Dissipative Particle Dynamics (DPD) and Langevin Dynamics (LD). It offers a broad variety of electrostatic algorithms, analysis tools and various other features such as the support of massively parallelized hardware architectures or GPU platforms.

- The package can be obtained free of charge under <http://essomd.org/wordpress/download/>.
- Be advised to also have a look at the ESPResSo manual to understand how it operates: <http://essomd.org/jenkins/job/master-doc/lastSuccessfulBuild/artifact/doc/ug/ug.pdf>

In the following, you will conduct coarse-grained simulations of polymers with LD to learn how to work with ESPResSo. The simulations focus on the ideal chain model and the chain with excluded volume interactions. You can either use the computers in the ICP CIP pool or install ESPResSo on your own computer.

4.2 Installing ESPResSo

Download and unpack the ESPResSo package version 3.2.0 (`espresso-3.2.0.tar.gz`). Follow the build procedure as given in the manual on pp. 23ff.

The `configure` script should be run with the option `--without-cuda` in order to avoid problems during compilation. After using `./configure` but *before* compiling with `make`, please uncomment the macros in `myconfig-sample.h` for `LENNARD_JONES` and rename it to `myconfig.h`.

4.3 Setting up and Running the Simulations

Download the template Tcl script `template.tcl` from the lecture website.

Examine the template script and also have a look at the manual (and perhaps on the test cases, too) to understand how to set up a polymer with Langevin Dynamics. You need harmonic springs with the spring constant $k = 10$ to connect the monomers. The temperature should be set to $T = 1$ and the friction coefficient of the Langevin thermostat to $\gamma = 1$.

Once the Tcl script is prepared, you can run the simulation with

```
$> /<install_dir>/Espresso template.tcl
```

4.4 Ideal Chain

Task	(4 points)
<ul style="list-style-type: none">• Perform simulations of an ideal coarse-grained polymer with Langevin Dynamics for different chain lengths $N \in \{10, 20, 30, 40, 50, 100, 200\}$ and determine the average radii of gyration $R_g(N)$.• Determine the parameter ν in the relation $R_g(N) \propto N^\nu$.	

4.5 Chain with Excluded Volume Interactions

Task	(4 points)
<ul style="list-style-type: none">• Simulate a coarse-grained polymer with the same interactions and parameters as given above. In addition, apply Lennard-Jones interactions to the monomers with $\epsilon = 1$, $\sigma = 1$, and cutoff radius $r_c = 2^{\frac{1}{6}}$. Shift the Lennard-Jones function such that the force is zero for $r = r_c$.• Repeat the simulations for the different values of N.• Determine ν as in the previous task.	